Problem Set 1

1)

Suppose an algorithm takes 5 seconds when the input size is 20,000. How long does it take if the input size is 100,000 under each of the following conditions:

The algorithm is linear. The algorithm is logarithmic The algorithm is cubic. The algorithm is n log n. The algorithm is quadratic. The algorithm takes constant time.

2) Consider the following C code:

 $\begin{array}{l} for(i = 0; \, i <= n; \, i += 2) \\ for(j = i; \, j < n; \, j ++) \\ foo(j); \end{array}$

Assume that foo(m) is a function of _(m) complexity. How many times is foo() invoked if n = 100? Circle the statements below which correctly describe the code's complexity.

 $O(n^{6})$ $\Omega(n^{6})$ $\Theta(n^{6})$ $O(n^{3})$ $\Omega(n^{3})$ $\Theta(n^{3})$ $O(n^{2})$ $\Omega(n^{2})$ $\Theta(n^{2})$ $O(n \log n)$ $\Omega(n \log n)$

 $\Theta(n \log n)$